



[18, 23, 33]).

[2, 9, 13]).

( )

[10, 12, 49]).

« ... »

) «... “ ” ( » [13].

« » [30], < > [47, 51].

**1.**

[17]: «

[2],

« ... »

—« »  
[6] :« ».  
: « ».  
( )  
« ».  
( )

— [6] :« ».  
».  
( )  
,  
;1) ;2)  
;3)  
( ) 1814  
:« »  
<...>  
» [12, .277].

2. ( ), ( )  
( ) « ».  
, [26, 37, 41, 44]), « » ( )  
( , [8, 27, 42, 46]). [10, 28]  
« »  
: « »  
, « ».  
—  
» n ( n « » )  
)

$n = n(t)$ ,

**3.**

[36, 42, 46],

5 %)

3

2014

[1, 27, 29, 34, 46]).

[3].

[3, 7].

[25, . 138–139].

[10, . 297–298]:

- 1)
- 2)
- 3)

[10, . 297]: «

[10, . 67–68]

- 1) «
- 2) «

167

3) « » , -  
 , .  
 , « » , »[10, .68],  
 « » ,  
 « » « » [10, .76]: «” -  
 ”  
 — :  
 ; , —  
 ( , ),  
 ».

4. ( : - )  
 - )  
 , ,  
 , - ,  
 , ,  
 , - ,

1. [22, c. 31]  
 , « » .  
 —

2. ( , )  
 — [4; 10, c. 44; 14; 16; 27; 31; 38])  
 (« » — , ).

3. [10, .268]  
 :«... GARCH ( , , )

4. [15, .454] ( . [43, 48, 52]),

5. ( , [11, .461] , — «  
 ».

6. [11, . 326–327] V R-  
 [45], [10, . 323–324]  
 [32, 40],

» ( [11, c. 586]).

[8]

5.

$$\Delta Y_t = Y_t - Y_{t-1} = F(\Delta Y_{t-1}) \varepsilon(t), \quad (1)$$

$$\Delta Y_{t-1} = Y_{t-1} - Y_{t-2} = F_{t-1}(\Delta Y_{t-2}) \varepsilon(t-1),$$

$$\Delta Y_{t-2} = Y_{t-2} - Y_{t-3} = F_{t-2}(\Delta Y_{t-3}) \varepsilon(t-2),$$

$$F(\Delta Y_t) = \sum_{j=1}^m f_j(\Delta Y_{t-1}), \quad (2)$$

$$f_j(\Delta Y_{t-1}) = f_j(\Delta Y_{t-1}, \Delta Y_{t-2}, \dots, \Delta Y_{t-m}), \quad (2)$$

$$\varepsilon(t) = \prod_{i=1}^k \varepsilon_i(t), \quad (3)$$

$$\varepsilon_i(t) = \varepsilon_i(\Delta Y_{t-1}, \Delta Y_{t-2}, \dots, \Delta Y_{t-m}), \quad (3)$$

$$\varepsilon(t) = \prod_{i=1}^k \varepsilon_i(t), \quad (3)$$

$$\varepsilon_i(t) = \varepsilon_i(\Delta Y_{t-1}, \Delta Y_{t-2}, \dots, \Delta Y_{t-m}), \quad (3)$$

$$\varepsilon(t) = \prod_{i=1}^k \varepsilon_i(t), \quad (3)$$

$$\varepsilon_i(t) = \varepsilon_i(\Delta Y_{t-1}, \Delta Y_{t-2}, \dots, \Delta Y_{t-m}), \quad (3)$$

$$\varepsilon(t) = \prod_{i=1}^k \varepsilon_i(t), \quad (3)$$

$$\varepsilon_i(t) = \varepsilon_i(\Delta Y_{t-1}, \Delta Y_{t-2}, \dots, \Delta Y_{t-m}), \quad (3)$$

$$\varepsilon(t) = \prod_{i=1}^k \varepsilon_i(t), \quad (3)$$

$$\varepsilon_i(t) = \varepsilon_i(\Delta Y_{t-1}, \Delta Y_{t-2}, \dots, \Delta Y_{t-m}), \quad (3)$$

$$\varepsilon(t) = \prod_{i=1}^k \varepsilon_i(t), \quad (3)$$

$$\varepsilon_i(t) = \varepsilon_i(\Delta Y_{t-1}, \Delta Y_{t-2}, \dots, \Delta Y_{t-m}), \quad (3)$$

$$\varepsilon(t) = \prod_{i=1}^k \varepsilon_i(t), \quad (3)$$

... ( , [5, 20]).  
 , [35, 36, 39, 42, 50].

( ,  $\varepsilon(t) \approx 0$  ) ,  $\varepsilon(t) \sim 1$ .  $\Delta Y_t$   
 ( ,  $\varepsilon(t)$  ),  $\varepsilon(t) \sim 1$ .  
 $F(\dots)$  (2),  $F(\varepsilon)$  (1).  $\Delta Y_t$

( , , ARIMA[21, c. 771–791]).

2 ( ) , [24],

( ) ,

« » . « »  
 « »

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